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2013年先進電機電子科技研討會—  
生物、醫學與電子科技的交流

電導心導管量測系統分析

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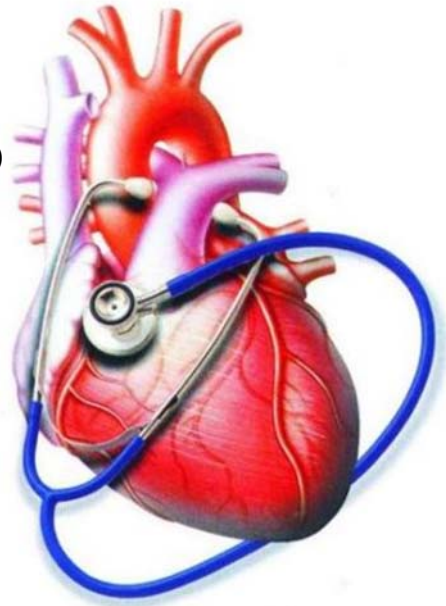
## Outline

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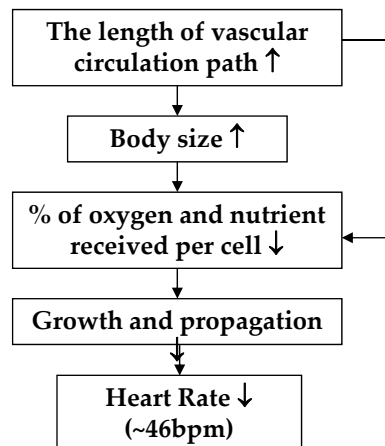
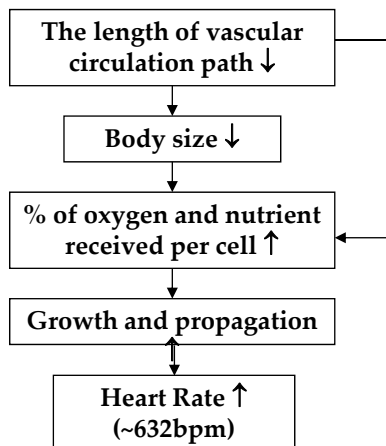
- Motivation
- Cardiology and Pressure-Volume Loop
- Introduction of Conductance Catheter Measurement System
- Issues of Conductance Catheter Measurement System
- Improvements and Achievement
- Conclusion

# Motivation

- ❑ Heart disease
  - ◆ More than 5,000,000 each year (USA)
  - ◆ One of the top ten death reasons (Taiwan)
- ❑ Heart-related Research
  - ◆ Gene
  - ◆ Medicine
- ❑ Animal Experiments
  - ◆ A method to quantitatively evaluate the performance of a heart is needed.

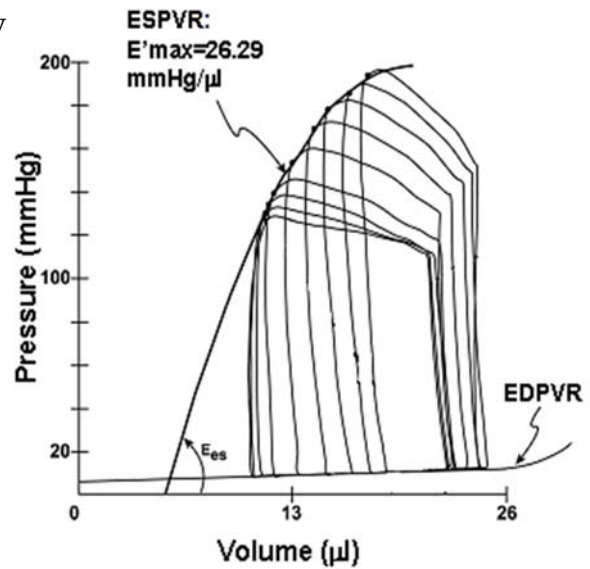


# Heart in Different Animals



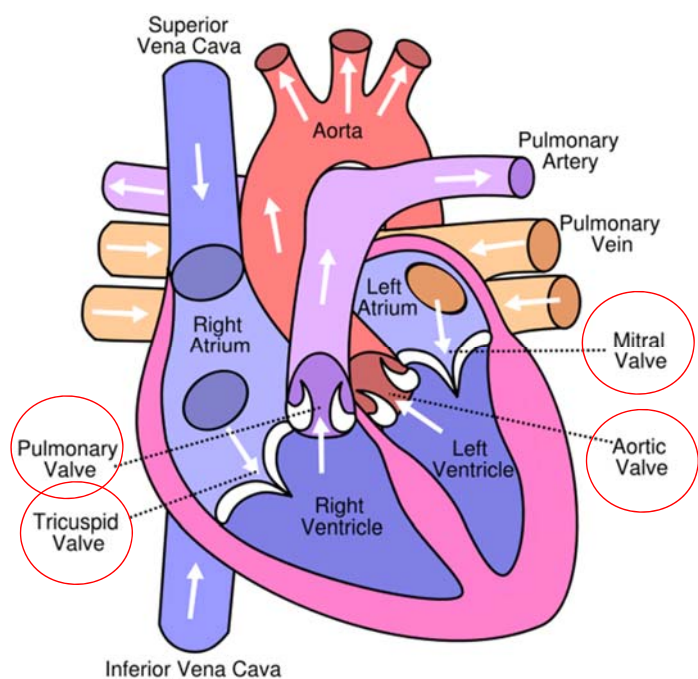
# Pressure-Volume Loops

- Pressure-volume loop analysis
  - ◆ Hemodynamic characterization of LV function
  - ◆ Myocardial physiologic function
- Baseline
  - ◆ Stroke volume
  - ◆ EDV & ESV
  - ◆ End-diastolic pressure
  - ◆ End-systolic pressure
- Dynamic
  - ◆ Preload
  - ◆ Afterload



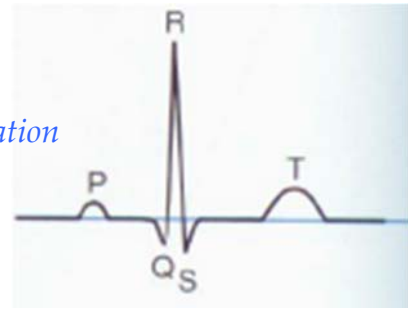
# Cardiac Anatomy

- Left and Right Atrium (LA & RA)
- Left and Right Ventricle (LV & RV)
- Aortic valve
- Pulmonary valve
- Mitral valve
  - ◆ bicuspid valve (二尖瓣膜)
- Tricuspid valve (三尖瓣膜)



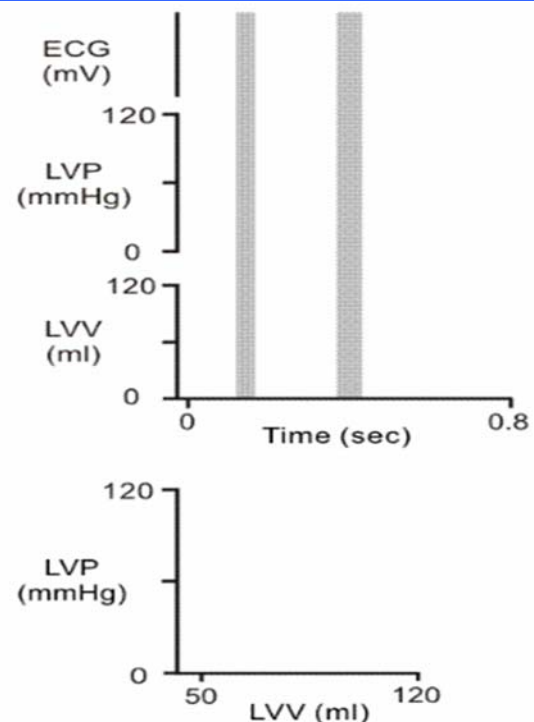
# Electrical Behavior of Cardiac Cells

- ❑ The *P wave* is produced by *atrial depolarization*
- ❑ The *QRS complex* primarily by *ventricular depolarization*
- ❑ The *T wave* by *ventricular repolarization*
  - ◆ The atrial repolarization is masked by QRS complex
- ❑ P-R interval is caused by conduction delay in the AV node
- ❑ S-T segment is related to the average duration of the plateau regions of individual ventricular cells
- ❑ A small additional U wave is sometimes recorded, which is due to slow repolarization of ventricular papillary(乳突肌) muscles.



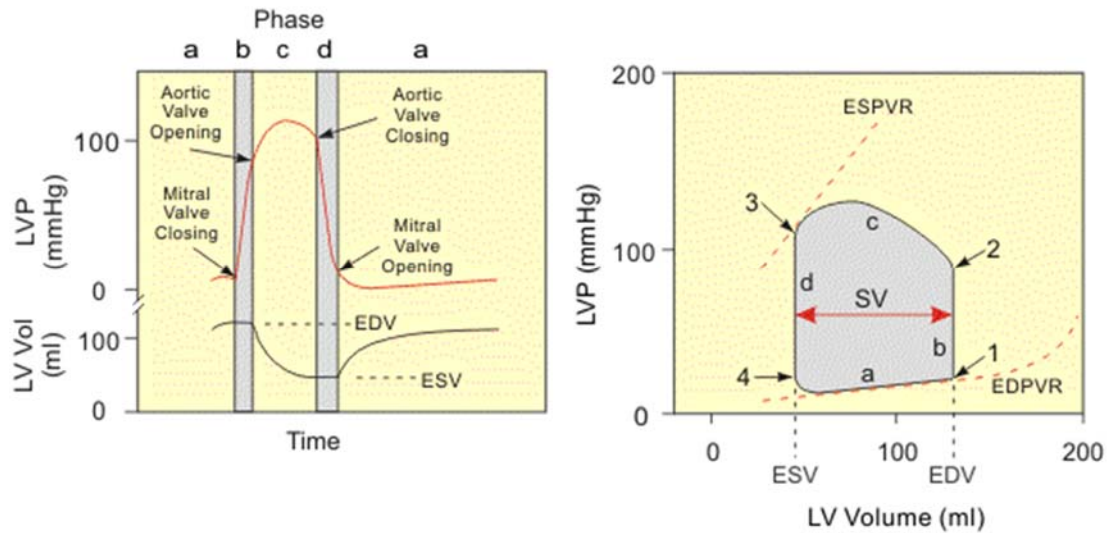
# Pressure-Volume Loop

- ❑ LV pressure-volume (PV) loops
  - ◆ pressure and volume information in the cardiac cycle diagram.
  - ◆ SV
    - the width of the loop
  - ◆ Ventricular stroke work
    - the area within the loop



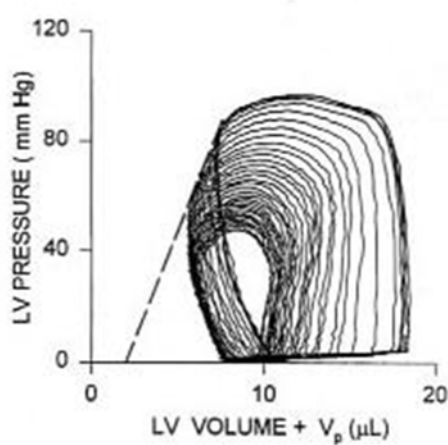
# Pressure-Volume Loop

- Phase a: ventricular filling (diastole)
- Phase b: isovolumetric contraction
- Phase c: ventricular ejection (systole)
- Phase d: isovolumetric relaxation

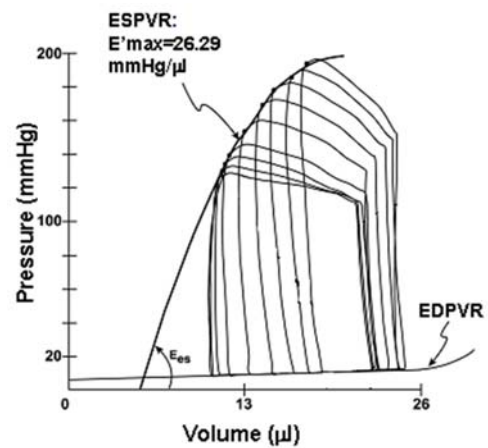


# Measurement of ESPVR and EDPVR

- ESPVR and EDPVR
  - ◆ dynamically changing preload and afterload



Decreasing preload



Increasing afterload

# Transgenic Mice

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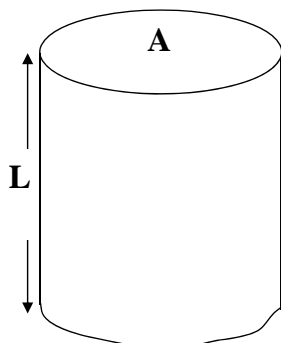
- Transgenic mice
  - ◆ Similar to human genes
  - ◆ Short generation
  - ◆ Cheap
- Issue of measuring mouse LV volume
  - ◆ Too small: LV ~ 15~80  $\mu\text{l}$  (0.015~0.08 cc)
  - ◆ Too fast: up to 600 bpm
- Conductance catheter measurement (1984)
  - ◆  $G=1/R$
  - ◆ proportional to volume

# The Relationship between Volume and Conductance

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- Volume  $Vol$

$$Vol = A \cdot L$$



- Conductance  $G$

$$G = \frac{1}{R} = \frac{A}{\rho L} \implies A = \rho GL$$

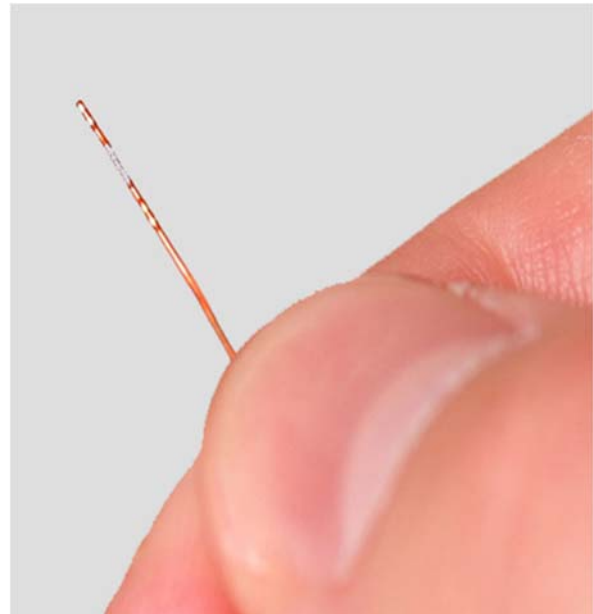
- The relationship between Volume and Conductance

$$Vol = (\rho GL) \cdot L = \rho L^2 G$$

- Linear relationship

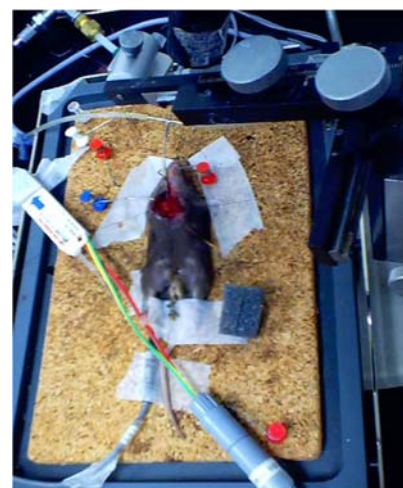
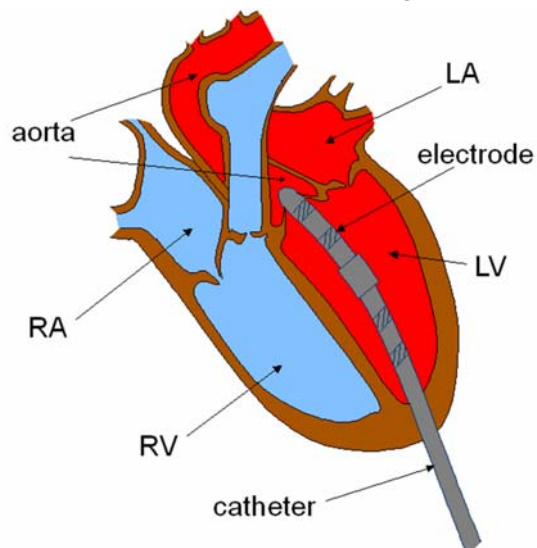
# Conductance Catheter

- ❑ Millar Instruments, Houston, Texas, USA.
- ❑ Conductance catheter (SPR-719)



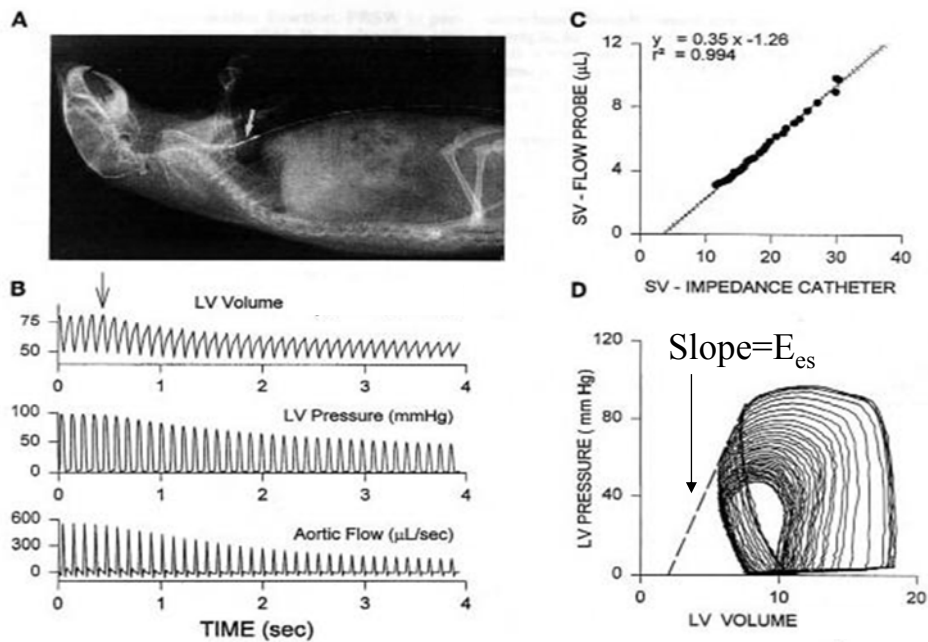
# Placement of Conductance Catheter

- ❑ A four-electrode conductance catheter
  - ◆ typically used in mice and rats
  - ◆ More electrodes for larger animals



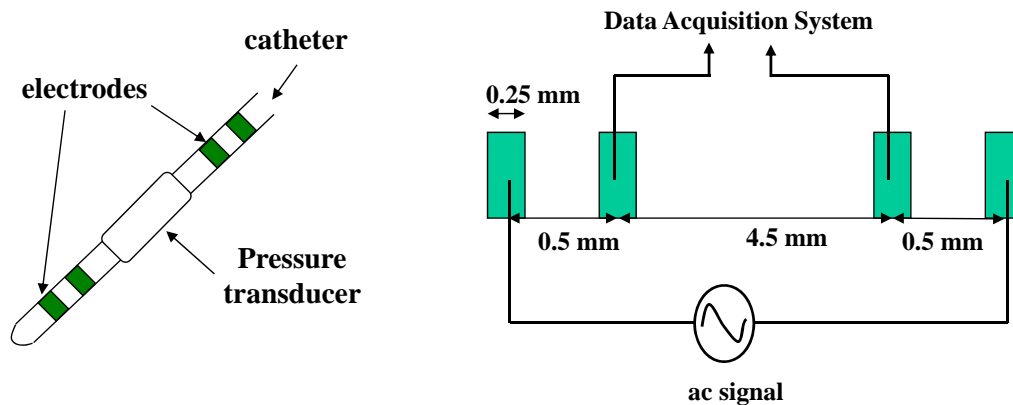


# Inferior Vena Caval Occlusion



# Illustration of Conductance Catheter Principle

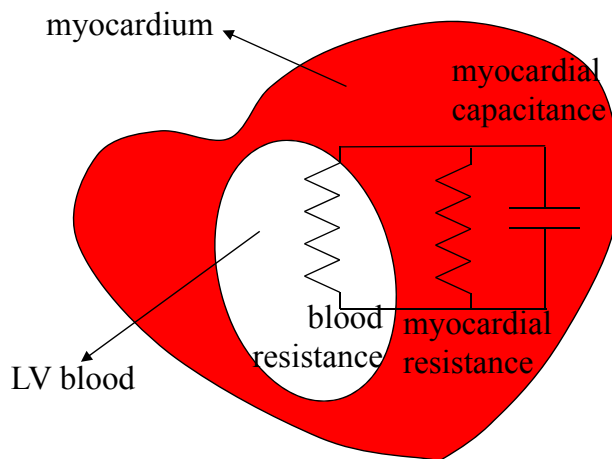
- Inject an ac current:  $I$
- Sensed the voltage:  $V$
- Conductance  $G = I/V$





# How to Convert Conductance to Volume?

- Both LV blood and myocardium are conductive.
  - ◆ Only the blood conductance is desired
  - ◆ Remove the myocardial contribution



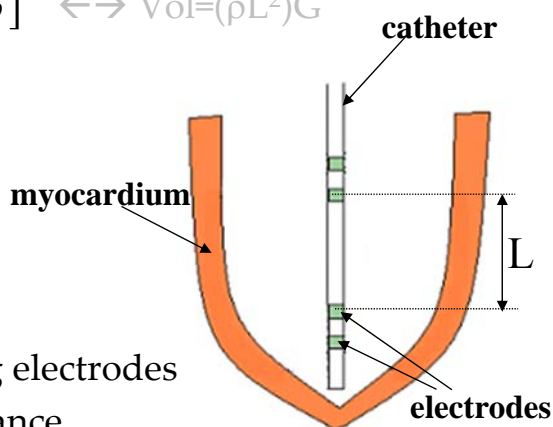
# Baan's Conductance-to-Volume Conversion Equation

- The conductance-to-volume conversion equation

$$Vol(t) = \frac{1}{\alpha} \rho L^2 [G_{meas}(t) - Gp] \leftrightarrow Vol = (\rho L^2) G$$

where

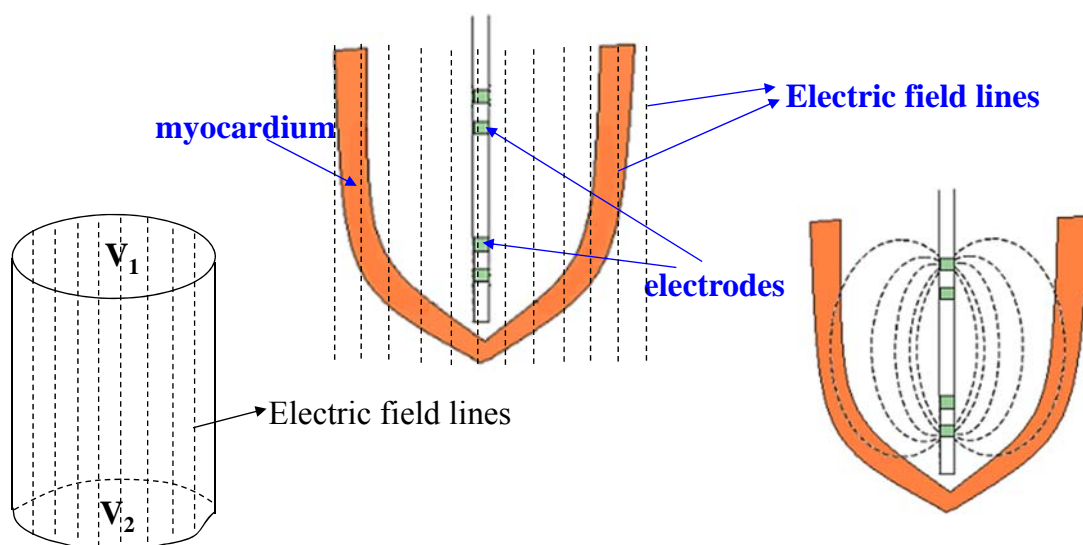
- Vol(t): volume
- $\alpha$ : calibration factor
- $\rho$ : blood resistivity
- L: distance between sensing electrodes
- $G_{meas}(t)$ : measured conductance
- Gp: myocardial conductance



# Accuracy of Conductance Catheter System

- Accuracy is mainly limited by three factors:
  - ◆ Assumption of a linear conductance-volume relationship
  - ◆ Deviation of the catheter position inside the LV
  - ◆ Estimation of myocardial contribution

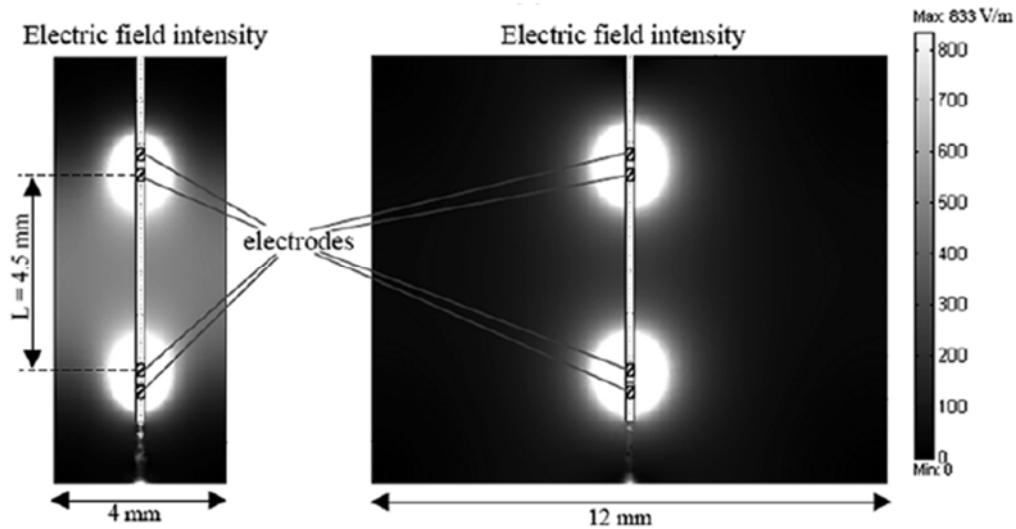
## Distribution of Electric field



- Inhomogeneous → nonlinear conductance-volume relationship

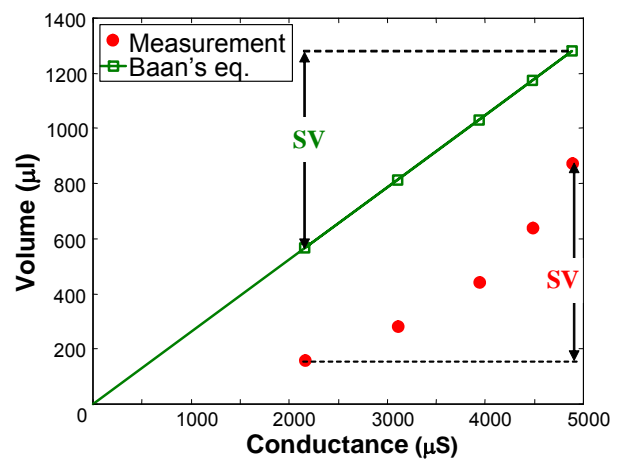
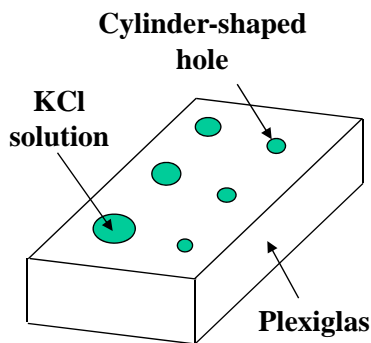
# Inhomogeneous Electrical Field: Conductance-Catheter Case

- ❑ The electric field generated by LV catheter electrodes is not uniform.

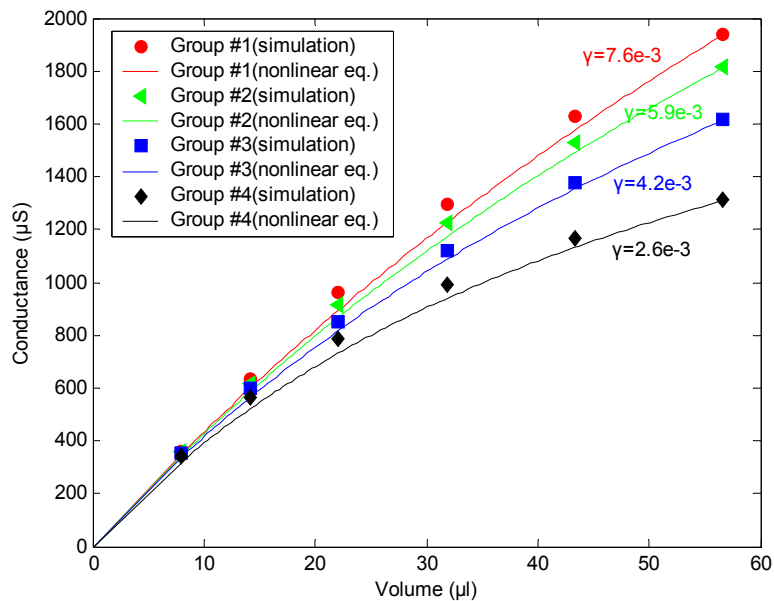


# Nonlinear Conductance-Volume Relationship

- ❑ Nonlinear relationship
- ❑ Baan's equation overestimates volumes



# Conductance-Volume Relationship v.s. Catheter Position



## Assumptions of Constant Myocardial Contribution

- The conductance catheter technique has long been said to have constant parallel conductance or current leakage into the myocardial wall throughout the cardiac cycle.
  - ◆ Previous studies only determine a single steady state value for the parallel myocardial contribution to conductance
    - Constant myocardial contribution

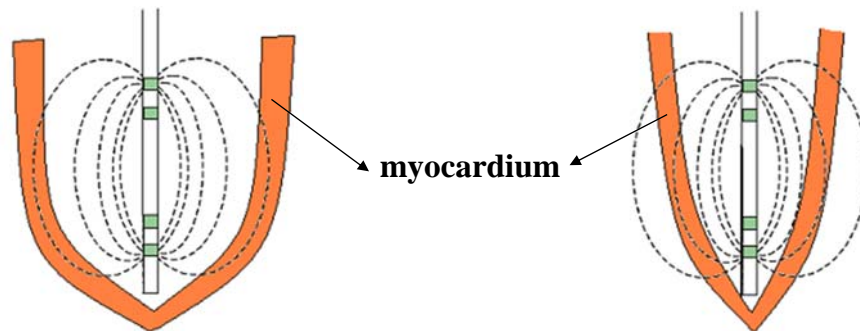
$$\text{Vol}(t) = (1/\alpha)(\rho L^2)(G_i(t) - G_p)$$

Not a function of time

# Time-Varying Myocardial Contribution

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- The fraction of total current reaching the myocardium varies between end-systole and end-diastole because the myocardium changes distance from the source electrodes
  - ◆ Time-varying myocardial contribution



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## Improvements & Achievements

## Nonlinear Approximation Equation

$$\alpha(g_b) = 1 - \frac{g_b}{\gamma}$$

$$\text{Vol} = \frac{1}{\alpha(g_b)} \rho L^2 g_b = \frac{\gamma}{\gamma - g_b} \rho L^2 g_b$$

- Use the SV to calibrate the system as Baan's equation, and then the empirical factor  $\gamma$  can be determined by

$$\gamma = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

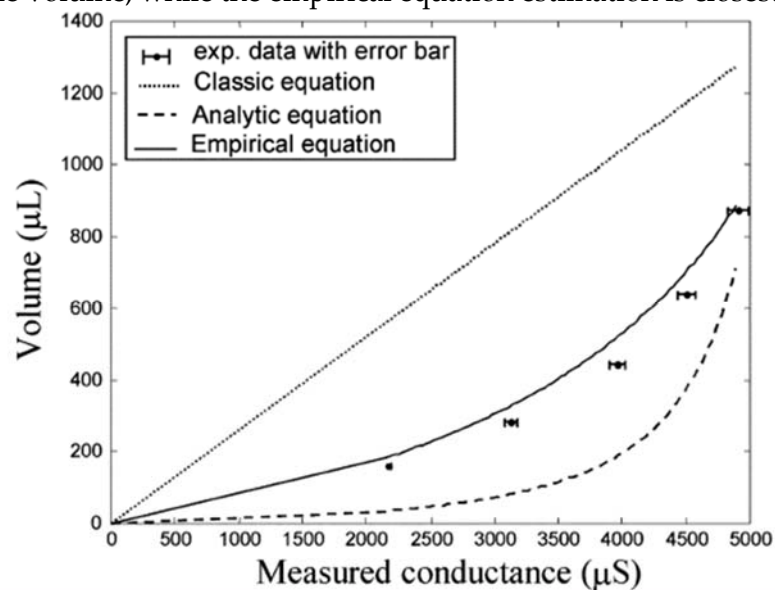
$$a = \text{SV} - \rho L^2 (g_{b-ED} - g_{b-ES})$$

$$b = -\text{SV} \cdot (g_{b-ED} + g_{b-ES})$$

$$c = \text{SV} \cdot g_{b-ED} \cdot g_{b-ES}$$

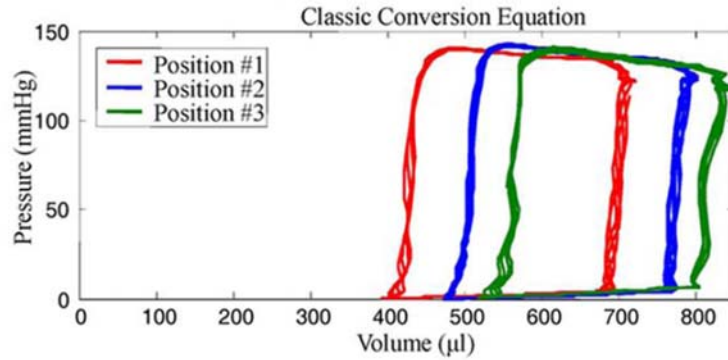
## Rat LV-Sized Volume Range

- A rat catheter (SPR-838, Millar Instruments) was used.
  - ◆ Baan's equation overestimates the volumes and the analytic equation underestimates the volume, while the empirical equation estimation is closest to the true volume.

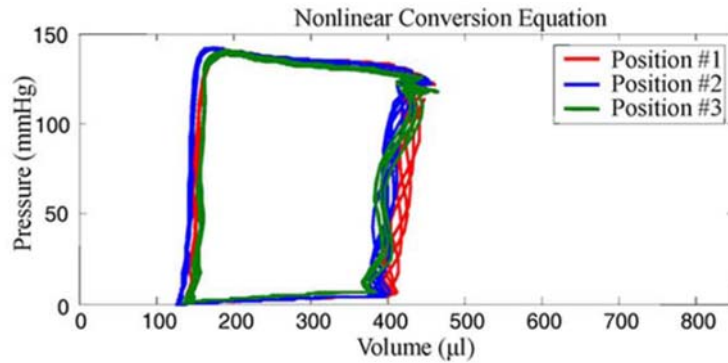


# In Vivo Rat Experiment

## □ Baan's Equation



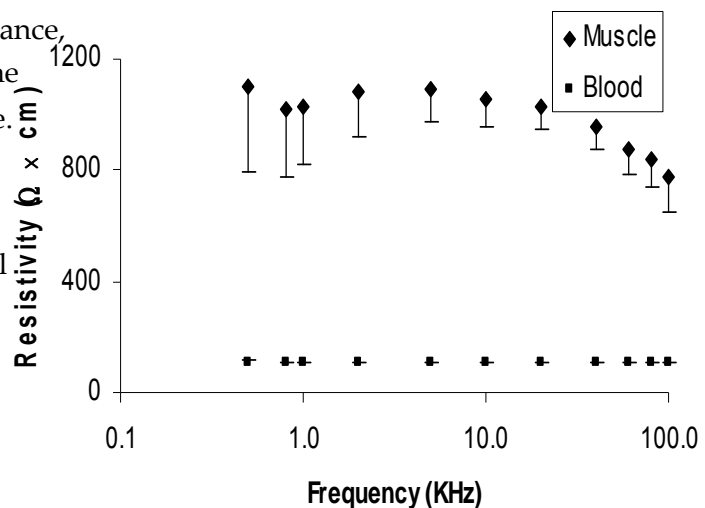
## □ Wei's Equation



# Electrical Property of Myocardium

□ For frequencies below 100 kHz, blood has been shown to be pure resistive, while myocardium has both resistive and capacitive properties.

- ◆ The capacitive property of myocardium makes the "apparent" myocardial resistivity decrease with increasing frequency.
- ◆ Instead of myocardial conductance, it is more appropriate to use the term of myocardial admittance.
- ◆ The distinguished capacitive property of myocardium can be used to separate myocardial contribution from blood conductance.





# Myocardial Conductance and Capacitance

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- In electromagnetism, the myocardial conductance  $g_m$  and myocardial capacitance  $C_m$  can be represented as

$$g_m = \frac{I}{V} = \frac{\oint_A J \cdot dA}{-\int_L E \cdot dl} = \frac{\oint_A \sigma_m E \cdot dA}{-\int_L E \cdot dl}$$
$$C_m = \frac{Q}{V} = \frac{\oint_A \varepsilon_m E \cdot dA}{-\int_L E \cdot dl}$$

where  $\sigma_m$  is myocardial conductivity,  $\varepsilon_m$  is myocardial permittivity,  $E$  is electric field,  $J$  is current density,  $I$  is current,  $Q$  is charge,  $A$  is the area of the surface enclosing the source electrode, and  $L$  is the path length for potential calculation.

# Myocardial Conductance and Capacitance

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- Assumed that both  $\sigma_m$  and  $\varepsilon_m$  are isotropic constants in the myocardium:

$$g_m = \sigma_m \frac{\oint_A E \cdot dA}{-\int_L E \cdot dl}$$
$$C_m = \varepsilon_m \frac{\oint_A E \cdot dA}{-\int_L E \cdot dl}$$

Hence, the well-known conductance-capacitance analogy is yielded:

$$\frac{C_m}{g_m} = \frac{\varepsilon_m}{\sigma_m}$$

- Either myocardial conductance  $g_m$  or myocardial capacitance  $C_m$  is once determined, the other one can be calculated by the analogy.

# Admittance Measurement Technique

- The admittance measurement consists of magnitude measurement and phase measurement.
- Magnitude ( $|Y_{meas}|$ ) + phase ( $\phi$ ) measurements  $\rightarrow$  admittance ( $Y_{meas}$ )

$$\text{Re}\{Y_{meas}\} = |Y_{meas}| \cos(\phi) = g_b + g_m$$

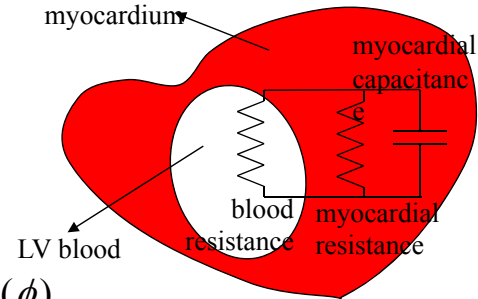
$$\text{Im}\{Y_{meas}\} = |Y_{meas}| \sin(\phi) = 2\pi f C_m$$

- ◆ Myocardial capacitance  $C_m$

$$C_m = \frac{|Y_{meas}| \cdot \sin(\phi)}{2\pi f}$$

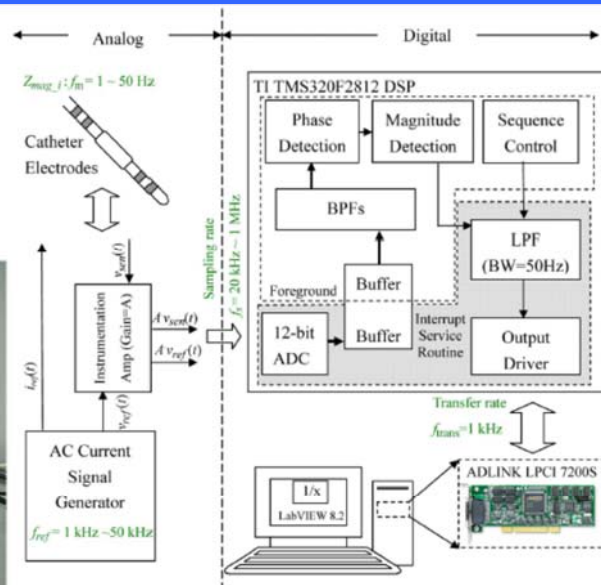
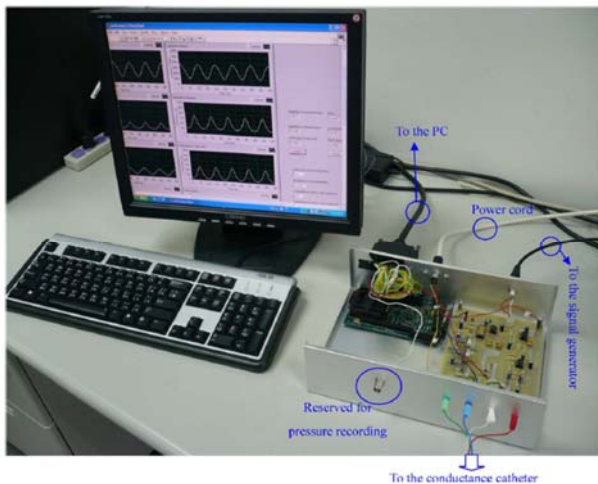
- ◆ The myocardial conductance  $g_m$

$$g_m = \frac{\sigma_m}{\epsilon_m} C_m = \frac{\sigma_m |Y_{meas}| \sin(\phi)}{2\pi f \epsilon_m}$$



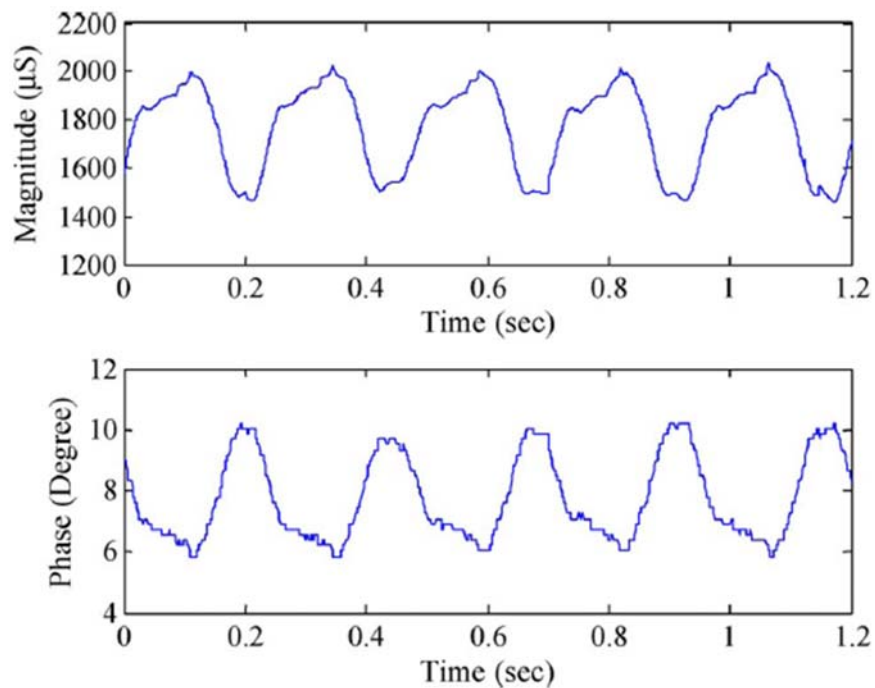
# DSP-Based Admittance Measurement System

- Real-time measurement
- Single frequency



[Ref] Chia-Ling Wei, Chieh-En Chen, I-Ta Tseng, and Chin-Hong Chen, "Real-Time DSP-Based Conductance Catheter Measurement System for Estimating Ventricular Volumes," *IEEE Transactions on Instrumentation and Measurement*, vol. 58, no. 10, pp. 3583-3591, 2009.

## In Vivo Measured Waveform



## Commercial PV Loop Measurement Systems

- ❑ Commercial conductance catheter measurement systems are available.
  - ◆ Millar Instruments, Houston, Texas, USA
    - Baan's Equation
  - ◆ Scisense, London, Ontario, Canada
    - Baan's Equation
    - Wei's Equation



# Conclusion

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- There are still many issues about the conductance catheter system.
  - ◆ Multidiscipline research
    - (Cardiac dynamics, Electromagnetism, Electronics, Digital image processing, Digital signal processing, *in vivo* & *in vitro* experiments, etc.)
  - ◆ Interesting

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